



# RailBeijing 2021



## Real-time Parameter Estimation Using An Unscented Kalman Filter

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Lab

Smart Public Transport



Lab

Digital Rail Traffic




# Outline of the presentation

- Introduction
  - EETC
  - Train motion model
- Framework
  - Unscented Kalman Filter
  - Driving Regime Identifier
  - Feature Extraction
- Case study
  - Data used
  - Results
- Conclusions

# Introduction I - EETC

## Energy-Efficient Train Control (EETC)

 Ease of  
implementation

(Relative)  
low cost

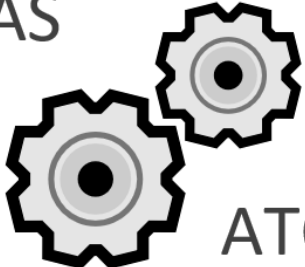


Key  
component

DAS

ATO

Energy-efficient  
timetabling



# Introduction II - Impact of EETC

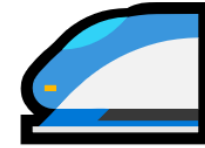
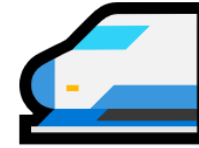
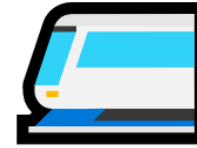
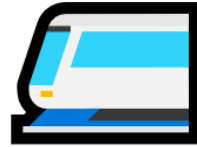
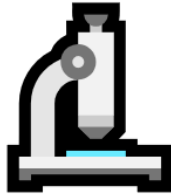


Energy  
consumption

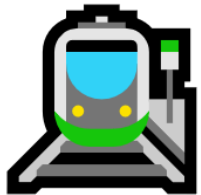


Train and  
track wear

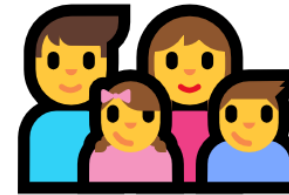
Precise  
operation



Capacity



Timetabling



Better  
service <sup>3</sup>

# Introduction III - EETC calibration



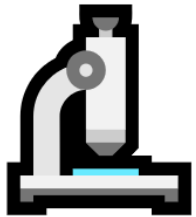
Offline calibration  
using historical data



Time  
variations



Not accurate in the  
long run or for all trains



Online calibration accurate  
only when coasting



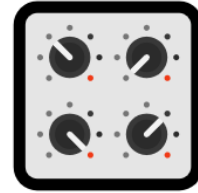
External  
factors

**Revolution:  
Train-tailored solutions**

# Introduction IV - Train motion model

$$\frac{dv}{dt} = f_t(v) - f_b(v) - r(v, s) - g(s)$$

It can reproduce train dynamics accurately if well calibrated



$s$  Location

$v$  Speed

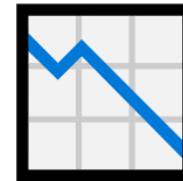
$f_t$  Tractive effort

$f_b$  Brake effort

$r(v, s)$  Running resistance

$g(s)$  Track  
resistance

Parameter  
Uncertainties

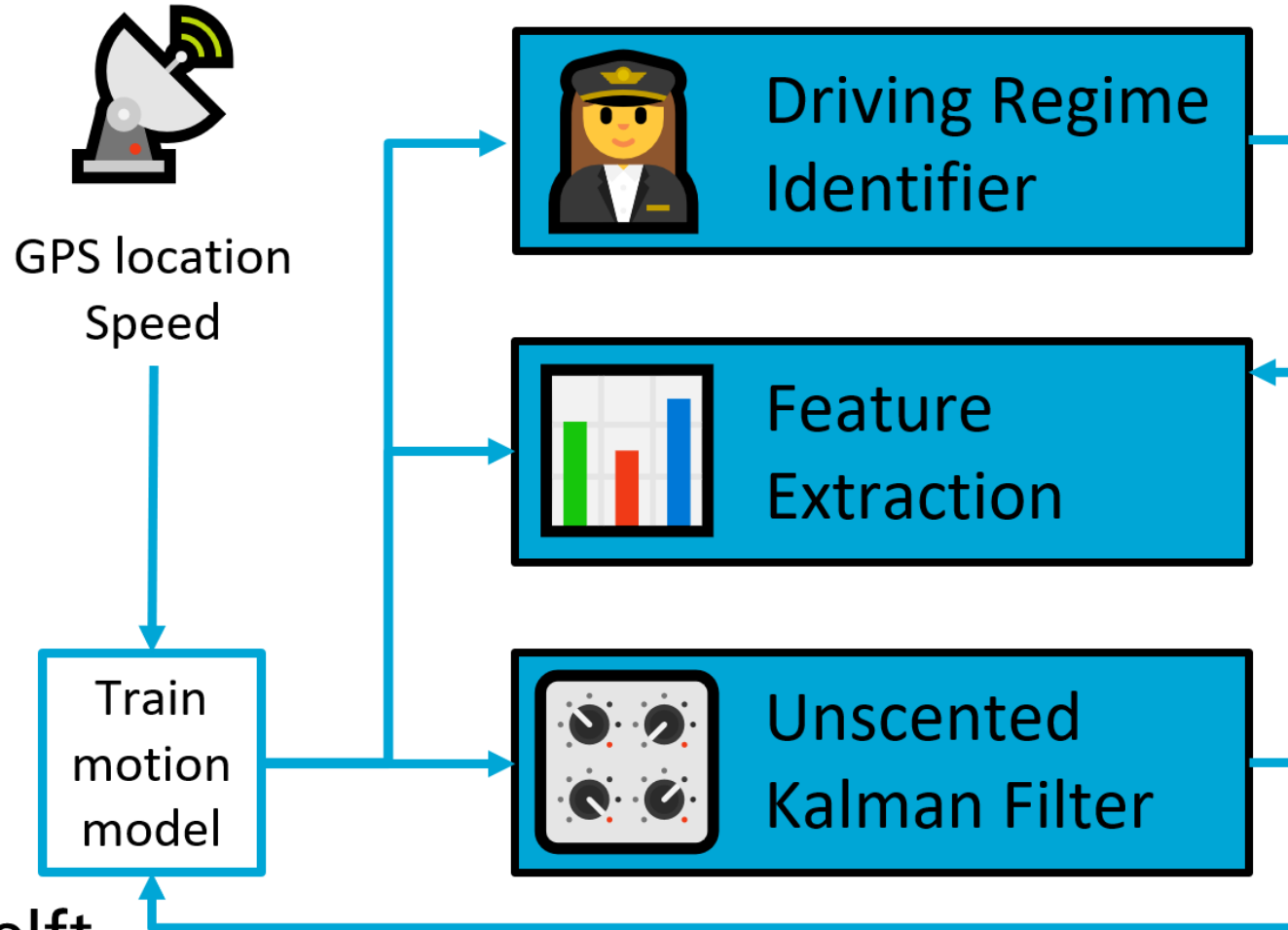


Spatiotemporal  
variability

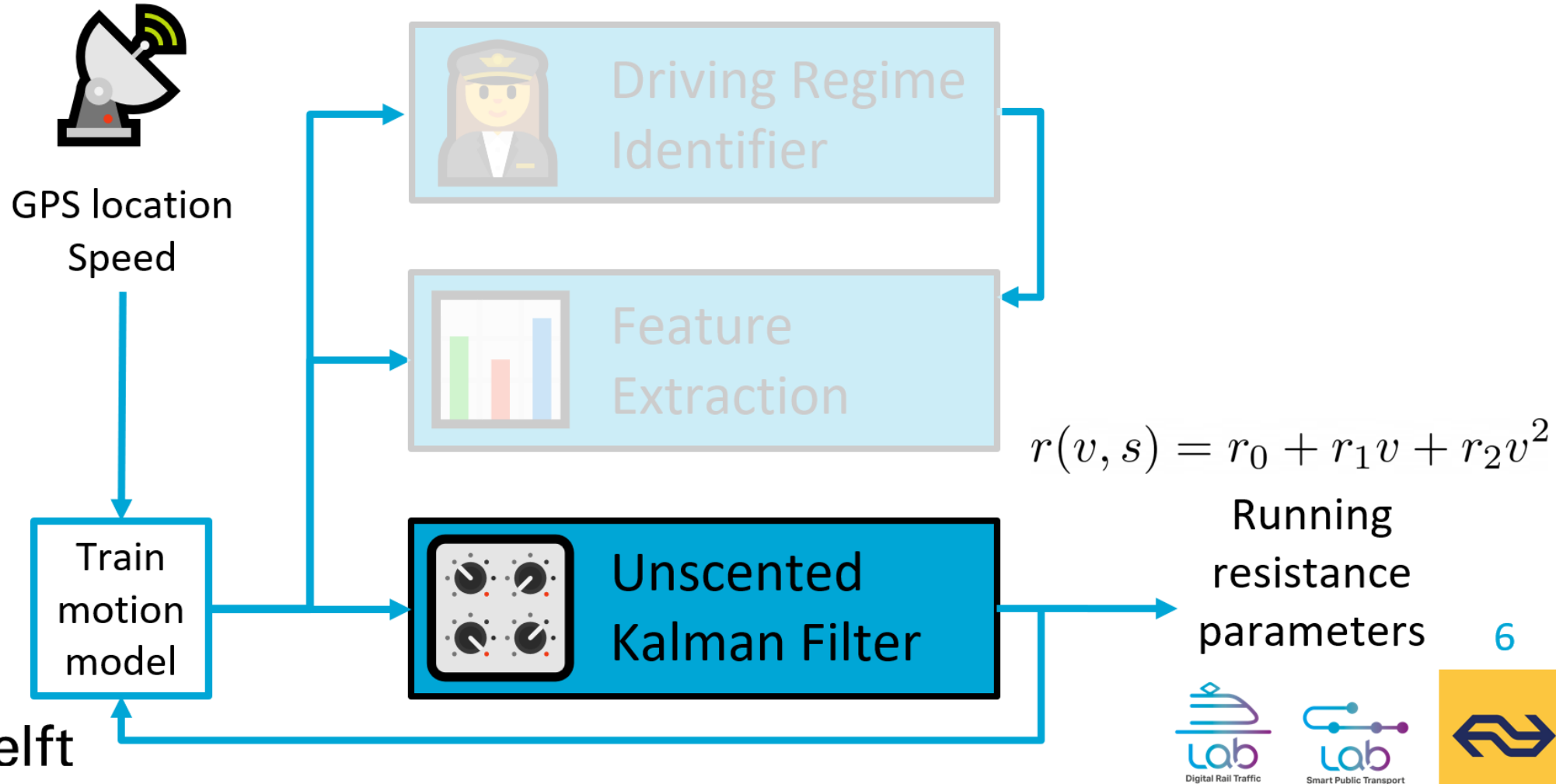
**Contribution:** Framework to calibrate  
EETC-based on-board tools in real time



# Framework



# Framework: Unscented Kalman Filter

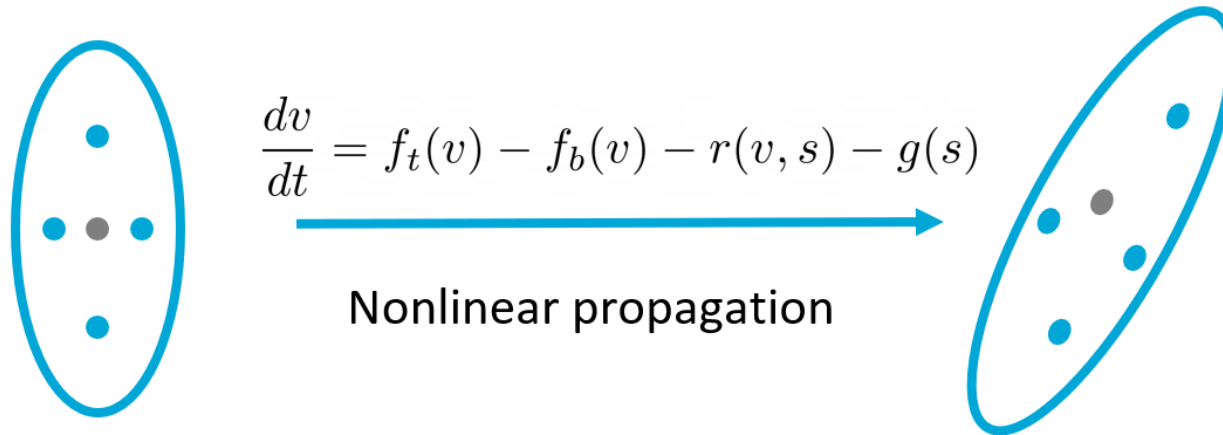




# Framework: Unscented Kalman Filter

**UKF**: State observer to estimate parameters of nonlinear systems

State statistics sampled deterministically and propagated nonlinearly

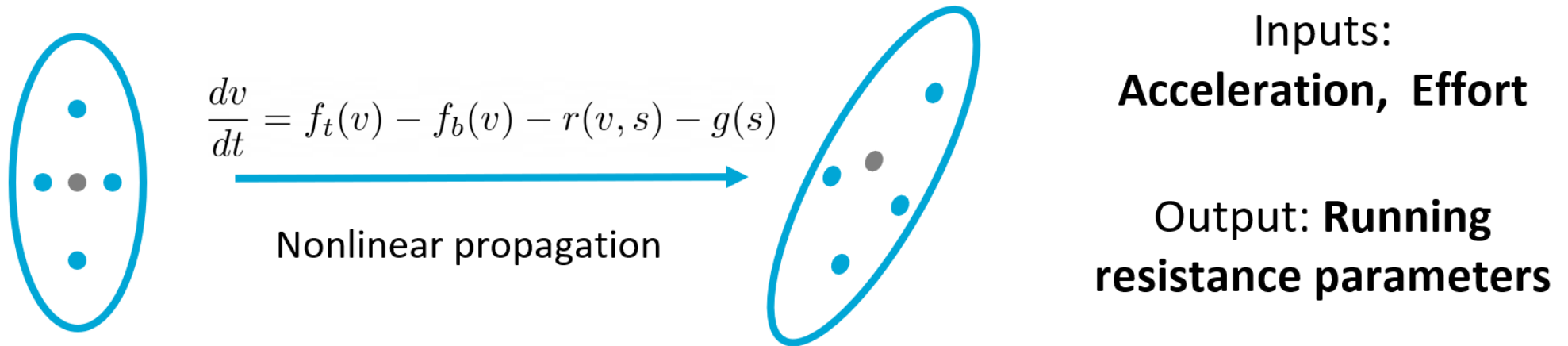


Julier and Uhlmann (1997). New extension of the Kalman filter to nonlinear systems

# Framework: Unscented Kalman Filter

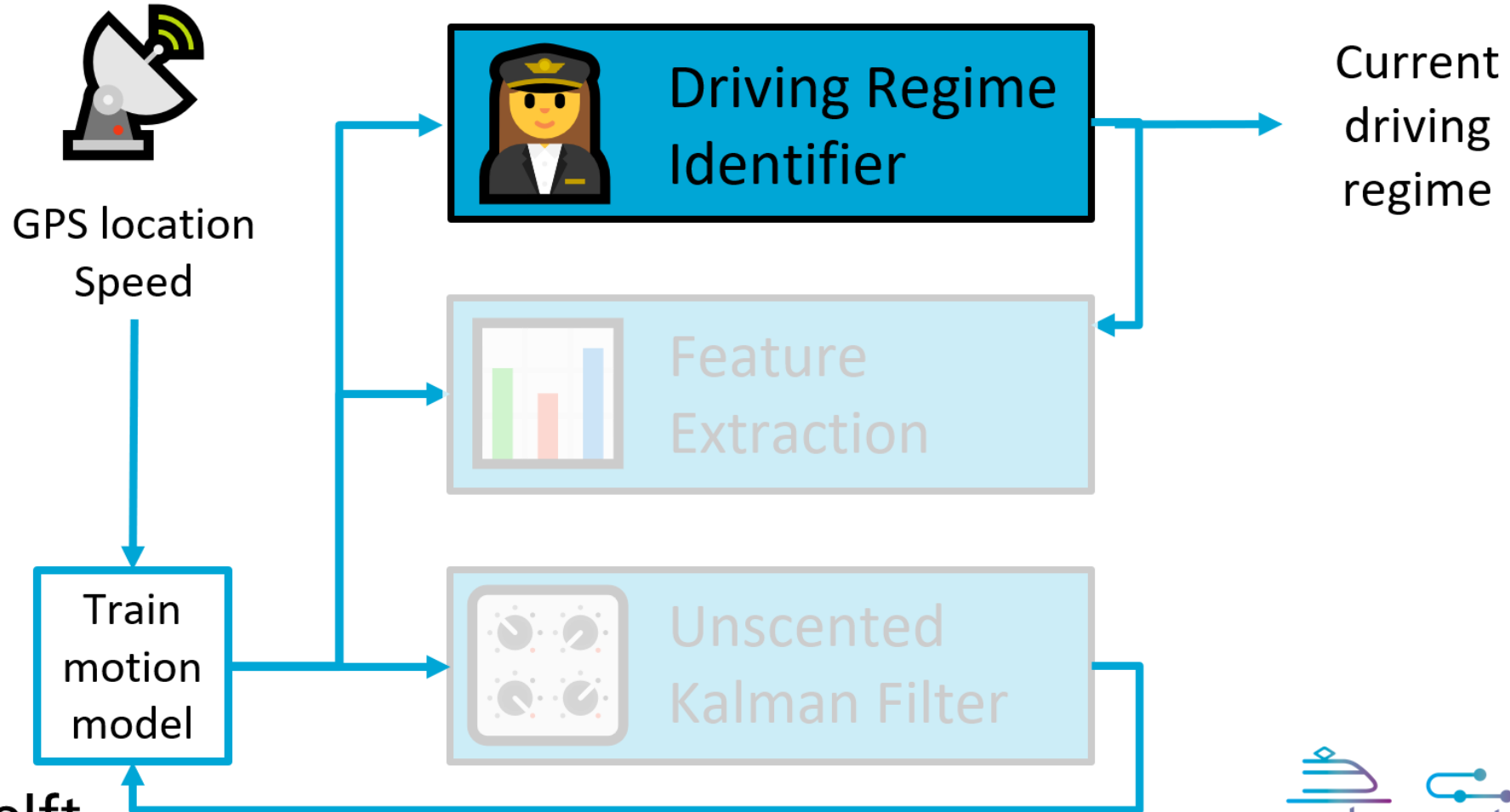
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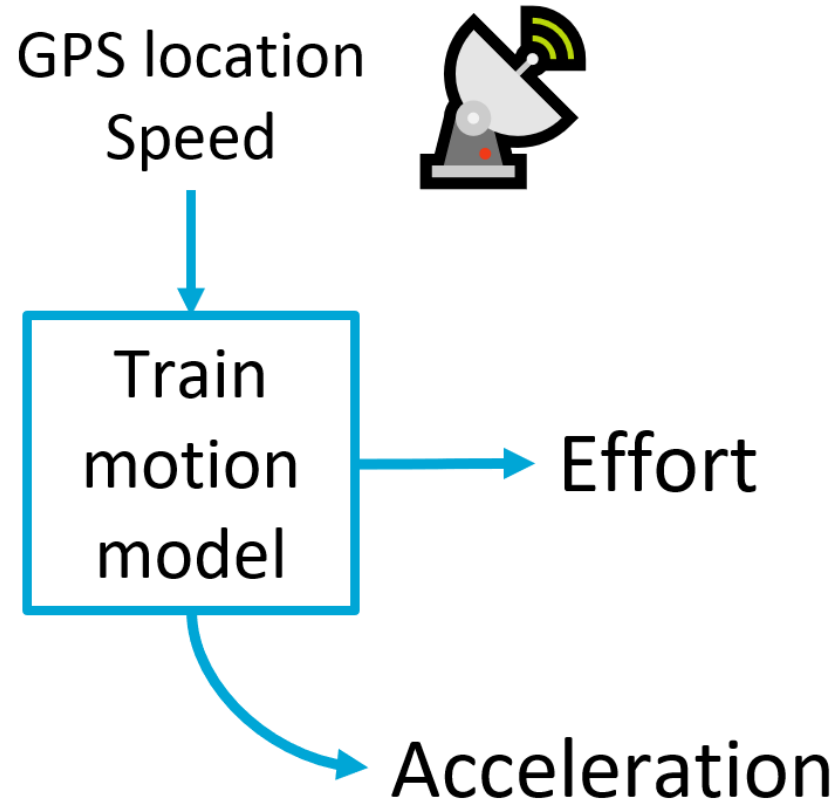


Julier and Uhlmann (1997). New extension of the Kalman filter to nonlinear systems

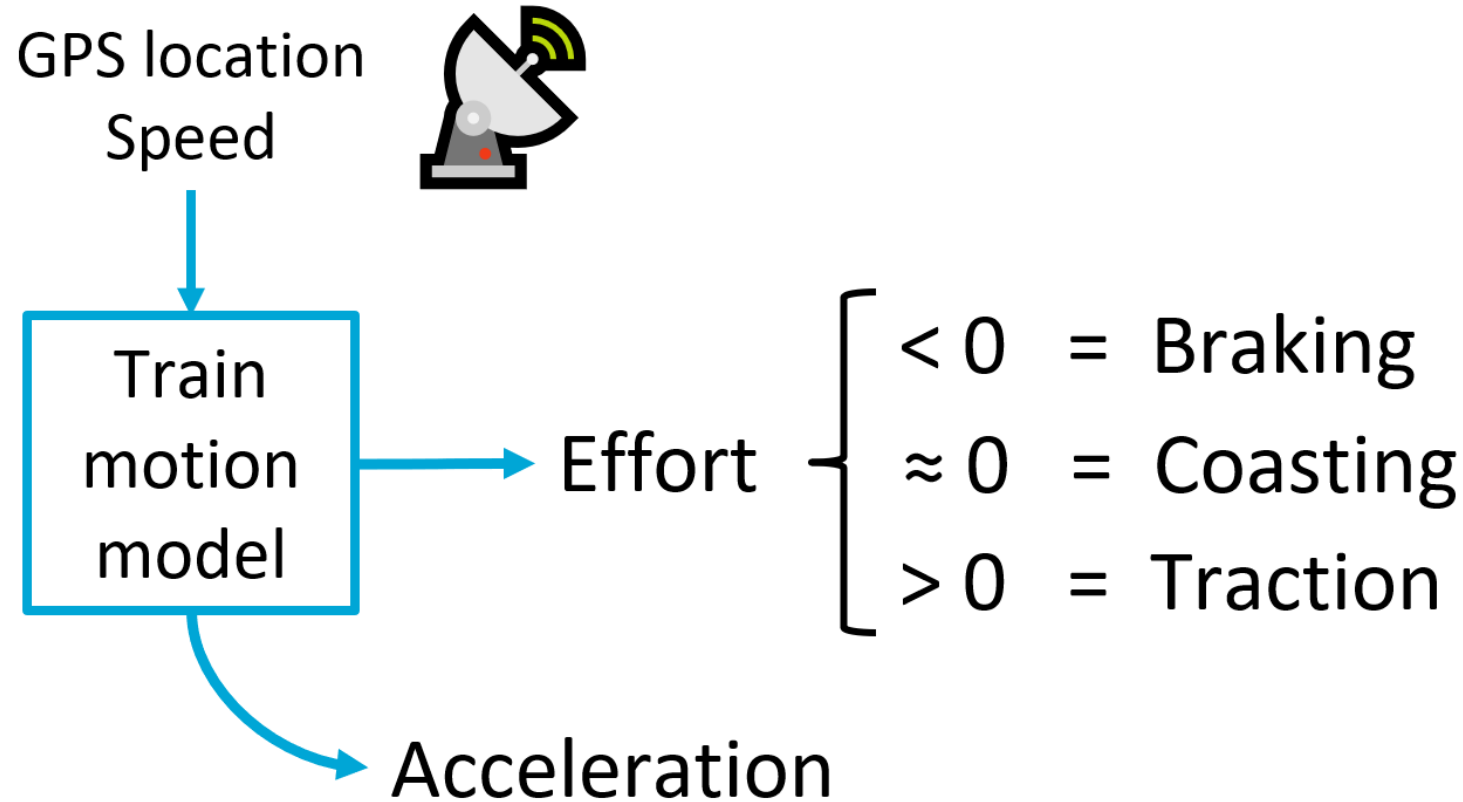
# Framework: Driving Regime Identifier



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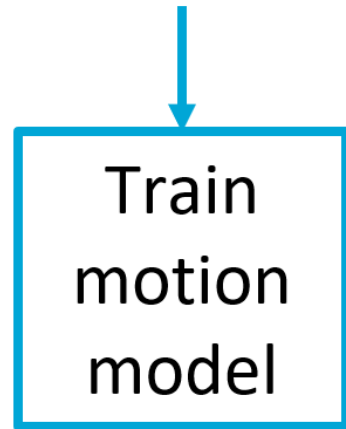


# Framework: Driving Regime Identifier



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GPS location  
Speed



Effort

$\left\{ \begin{array}{ll} < 0 & = \text{Braking} \\ \approx 0 & = \text{Coasting} \\ > 0 & = \text{Traction} \end{array} \right.$

Acceleration  $\approx 0$  = Cruising



# Framework: Driving Regime Identifier

GPS location  
Speed



Output: **Current  
driving regime**



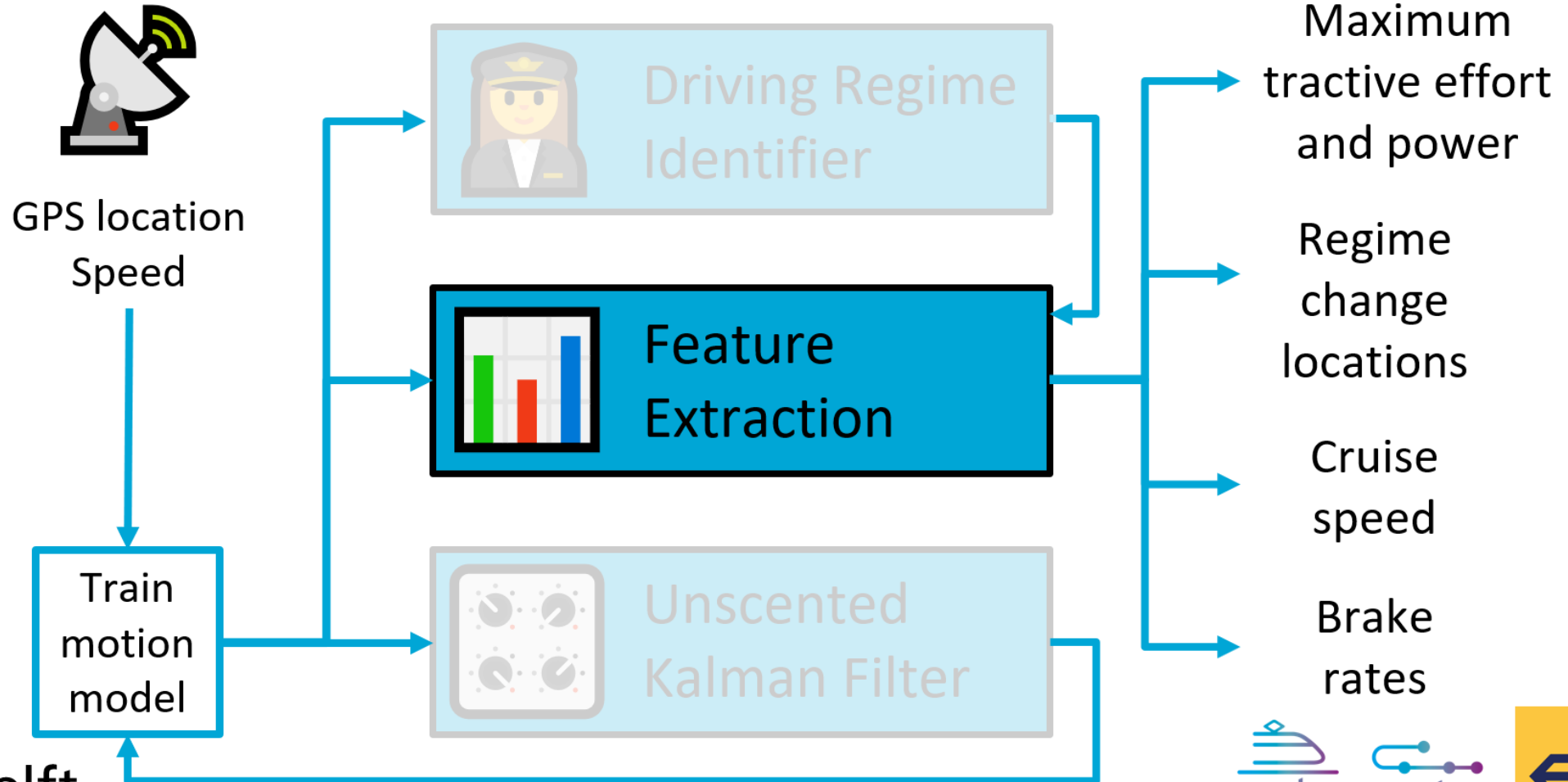
Train  
motion  
model

Effort

$\left\{ \begin{array}{ll} < 0 & = \text{Braking} \\ \approx 0 & = \text{Coasting} \\ > 0 & = \text{Traction} \end{array} \right.$

Acceleration  $\approx 0$  = Cruising

# Framework: Feature Extraction



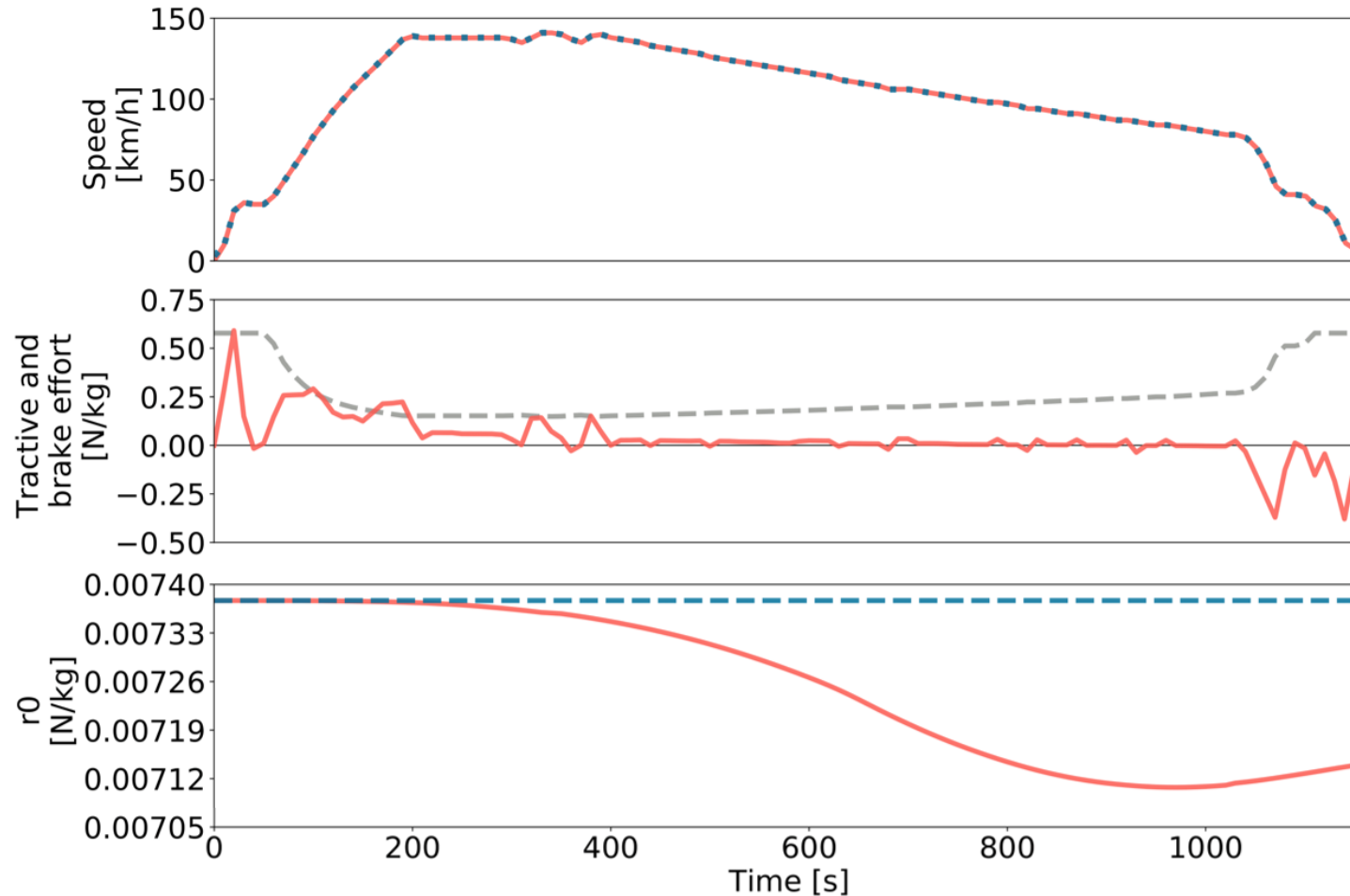


# Case Study

- 67 train trajectories of the same rolling stock unit
- Line Eindhoven – Den Bosch
- Track mostly flat
- Input data: Speed and location measurements
- Sampling rate 10s

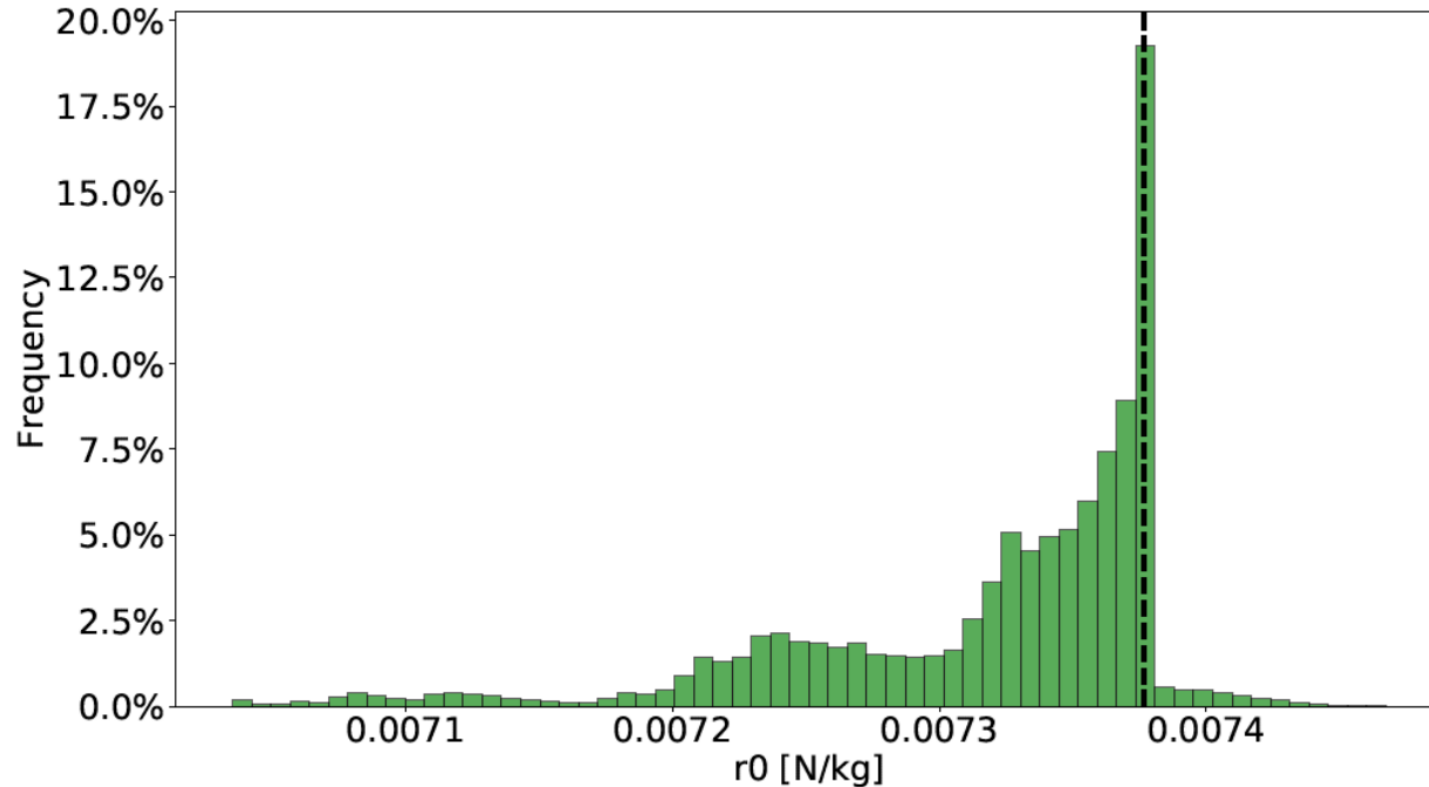


# Results I: Parameter Estimation



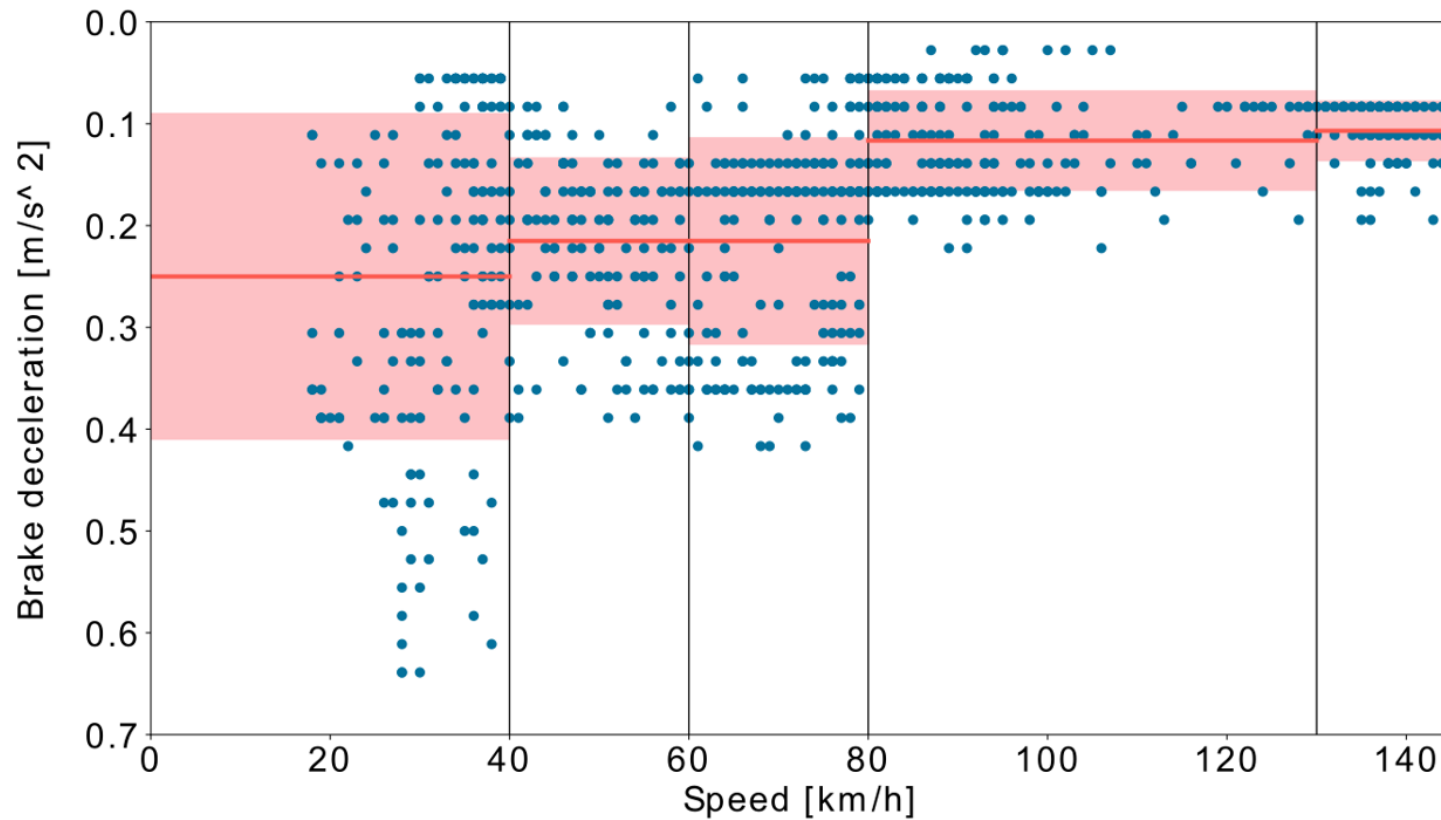
UKF can track speed measurements and estimate the running resistance parameters

# Results II: Running resistance parameters



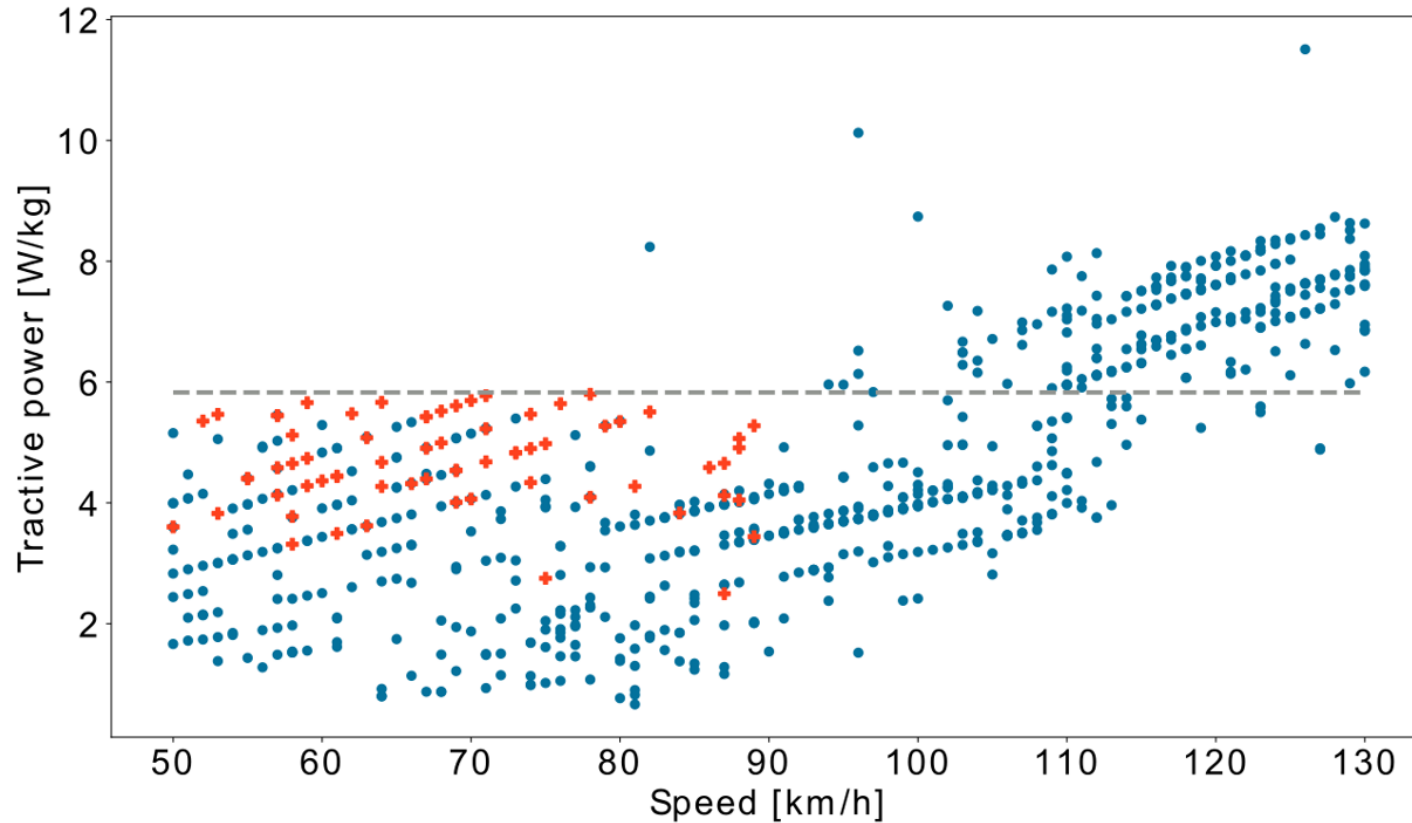
Manufacturers tend to overestimate the value of the running resistance parameters

# Results III: Brake rates



3 different  
brake rates  
along the 5 ATP  
braking speed  
steps

# Results IV: Maximum tractive power



Manufacturer upper bound is accurate

We observe a change of power station after departure station

# Conclusions

- Parameter estimation framework for EETC applications
- Performance tested using real data in a case study
- Framework can determine
  - Running resistance parameters
  - Current driving regime
  - Bounds and statistics of input parameters of EETC applications
- Limitations:
  - No applied effort measurements lead to lower accuracy
  - UKF internal parameters difficult to tune
  - Low measurement sampling rate

# Contact details + Download the paper

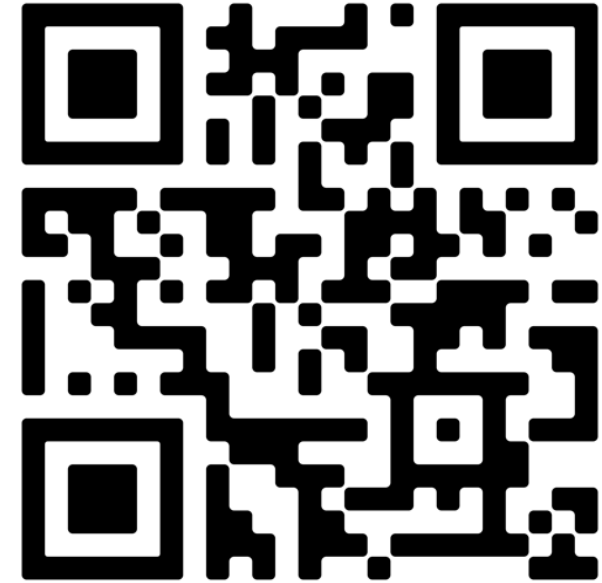
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[www.tudelft.nl/en/ceg/drtlab](http://www.tudelft.nl/en/ceg/drtlab)  
<http://smartptlab.tudelft.nl/>



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Paper & Slides

# Variability sources I: Traction

$$\frac{dv}{dt} = f_t(v) - f_b(v) - r(v, s) - g(s)$$





# Variability sources II: Brake

$$\frac{dv}{dt} = f_t(v) - f_b(v) - r(v, s) - g(s)$$



# Variability sources III: Resistance

$$\frac{dv}{dt} = f_t(v) - f_b(v) - r(v, s) - g(s)$$



$$r(v, s) = r_0 + r_1 v + r_2 v^2$$

# Variability sources IV: Track

$$\frac{dv}{dt} = f_t(v) - f_b(v) - r(v, s) - g(s)$$

